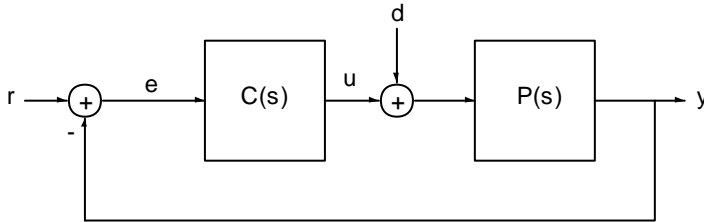


Problem 1:

For the feedback system shown below, compute the transfer functions e/r , u/d , y/d , e/d .

**Problem 2: (Low Bandwidth Controller)**

For the feedback system of Problem 1, suppose $P(s) = 1/(s + 0.5)$.

- When $C(s) = K$, design K so that the loop crossover frequency (i.e., ω : $|P(j\omega)C(j\omega)| = 1$) is 0.2rad/s . What is the contribution of a constant unit disturbance to the output?
- When $C(s) = K(Ts + 1)/s$, design K, T so that the crossover frequency is 0.2rad/s and the phase margin (i.e., the difference between the loop angle and -180 at the crossover frequency, $\angle P(j\omega_c)C(j\omega_c) + 180$) is at least 60° . What is the contribution of a constant unit disturbance to the output?

Verify in MATLAB, using `step(feedback(P,0.54),feedback(P,C))`

Problem 3: (High Bandwidth Controller)

For the feedback system of Problem 1, suppose $P(s) = 1/(s + 0.5)$.

- When $C(s) = K$, design K so that the loop crossover frequency (i.e., ω : $|P(j\omega)C(j\omega)| = 1$) is 20rad/s . What is the contribution of a constant unit disturbance to the output?
- When $C(s) = K(Ts + 1)/s$, design K, T so that the crossover frequency is 20rad/s and the phase margin (i.e., the difference between the loop angle and -180 at the crossover frequency, $\angle P(j\omega_c)C(j\omega_c) + 180$) is at least 60° . What is the contribution of a constant unit disturbance to the output?

Verify in MATLAB, using `step(feedback(P,20),feedback(P,C))\`

Problem 4: (Optional, 10% bonus)

Select a suitable sampling rate and use your favorite continuous-to-discrete conversion method to discretize the controllers of P.2 and P.3 (obtain discrete-time “equivalents”). Simulate the responses in SIMULINK (discrete-time controller, continuous time system).